

# A Neural Network Based Method for Cost Estimation 63/20kV and 132/20kV Transformers

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# ABSTRACT

Power transformers are one of the most important components in electrical network which has a vital role in electrification. Large numbers of transformers are required while expanding the electrification. In initial steps of evaluating project, having an estimated cost in short time can be beneficial. Around 15% of investment in transmission system goes towards transformer and since the major amount of transformers costs is related to its raw materials, cost estimating process can be an issue of crucial importance.

In this paper, a new method is presented to estimate transformers pricing. In order to this aim, a unique Multi-Layer Perceptron (MLP) neural network has been designed for two various types of 63/20kV and 132/20kV transformers in Iran. In the next stages the cost of the transformer is estimated, finding suitable coefficients for the weight of copper, iron, transformer oil (that are MLP neural network outputs) and a constant coefficient that is related to manpower cost and other components of transformer costs. The requirement training data for MPNN are the obtained from the transformers made by Iran-Transfo Company during last 4 years.

**KEY WORDS:** Artificial Neural Network (ANN), Back Propagation (BP), cost estimating, power system, transformer design.

## INTRODUCTION

The transformers are one of the most important components of the power systems, which have a vital role in transmission and distribution of electrical power. The same way that continuous performance of transformers is necessary to retain the network reliability, forecasting its costs is also important for manufacturer and industrial companies. In initial steps of evaluating project, having an estimated cost of a short period is useful, but evaluating initial costs, by customary method is a time-consuming process. Progresses in design, manufacturing and costs estimating of transformer have been surveyed in various studies [1-6].

Designing a transformer is carried out to access all dimensions, based on the desired characteristics, available standards, and access to lower cost, lower weight, lower size and a better performance. Various methods have been studied and some techniques such as geometric programming [1], simulated annealing technique [2], genetic algorithm, finite element method [3], neural network [4], and some other new techniques [5-6] were performed to design a transformer. The major amount of transformer's costs is related to its raw materials. Thus, row materials play an extremely pivotal role in costs estimating process.

In recent years, neural network have quite often been used in the field of transformers design. Determining insulation aging [7], and the time left from life of transformers oil [8], estimation of transformers oil parameter [9], transformers protection [10], and core wire choice in order to reduce the cost [11] are few topics that has been carried out.

In this paper, a new method is introduced to estimate transformers costs by means of Artificial Neural Network (ANN) and based on data that were extracted from one transformer manufacturer (IRAN-TRANSFO Co.). In order to this, a unique Multi-Layer Perceptron (MLP) neural network has been designed for two various types of 63/20kV and 132/20kV transformers in Iran and the cost of the transformer is estimated finding suitable coefficients for the weight of copper, iron and transformer oil (that are MLP neural network outputs) and a constant coefficient that is related to manpower cost and other components of transformer costs. Then, artificial neural networks are revised, then the ANN configuration is applied and it has been trained using the data of IRAN-TRANSFO Co for estimating transformer costs. Finally, resulted outputs of trained neural network are presented which will prove the accuracy of price estimation and consumed material.

#### ARTIFICIAL NEURAL NETWORK (ANN)

#### **ANN Structure**

A neural network is determined by its architecture, training method, and exciting function. Architecture, determines the pattern of connections among neurons. Network training changes the values of weights and biases (network parameters) in each step in order to minimize the mean square of output error. Since feed-forward neural networks or Multi-Layer Perceptron (MLP) ANNs is used in engineering applications such as load forecasting, nonlinear control, system identification, and pattern recognition [12-13], thus in this paper, multi-layer perceptron network (with four

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inputs, three outputs and a hidden layer) with back-propagation training algorithm is used. Since, this method is based on error gradient method, differential function is used. Thus, differentiable functions like Sigmoid, hyperbolic tangent must be used and in this case nonlinear sigmoid transformation function is used. Fig. 1 shows the MLP network that is used in this study.



Fig. 1. Artificial Neural Network

#### Input and Output of ANN

The required data are the data which have been accumulated by IRAN-TRANSFO Co. in last four years, and are used for estimating the iron, copper, and oil weight of transformers and consequently transformer costs are estimated by the proposed method (in various installation height and temperature with different short-circuit impedance and volt per turn). The schematic of the presented method can be shown by Fig. 2.



Fig. 2. Schematic of Inputs and Outputs

#### **Training of ANN**

In order to train a neural network we need data for training. The last four years transformer data obtained from IRAN-TRANSFO Co. is used. These data for the transformers 63/20kV and 132/20kV are shown in the Tables II, III and IV, V respectively.

An Artificial Neural Network MLP-Multi Layer Perceptron with back-propagation (BP) method can be used for reaching this goal. To determine weights and biases of neural network, a number of a different data are needed to learn the network. In table I structure of neural network and it training parameter are shown.

TABLE I			
ARCHITECTURE OF ANN AND TRAINING PARAMETERS			
Architecture of ANN			
The number of layers	3		
The number of neuron on the layers			
Input	4		
Hidden	2		
Output	3		
The initial weights and biases	Random		
Activation functions	Sigmoid		
Training parameters			
Learning rule	back-propagation		
Learning rate	0.01		
Momentum constant	1		
Mean squared error	1e-4		

#### **BP FORMULATION FOR TRANSFORMER**

With the help the artificial neural network of multi-layer perceptron with back propagation algorithm, a hidden layer is used for weight estimation of transformer's iron, oil, copper as shown in Fig. 1. Relation of multi layer perceptron, by back propagation algorithm is as following in equation (1)-(7): 1. Supremacy Path

$$a_{o}(\vec{k}) = P(\vec{k}) \tag{1}$$

$$a_{m+1}(k) = f_{m+1}(W_{m+1}(k)a_m(k) + b_{m+1}(k))$$
(2)

$$m = 0, 1, \dots, M - 1$$

$$a(k) = a_{M}(k)$$
(3)

$$e(k) = t(k) - a(k)$$
(4)

$$e(k) = l(k) - d(k)$$

$$S_{M}(k) = -2f'_{M}(n_{M}(k))e(k)$$
(5)

$$S_{m}(k) = f'_{m}(n_{m}(k))(W_{m+1}(k))^{T}S_{m+1}(k)$$

$$m - M - 1 M - 2 - 21$$
(6)

$$m = M - 1, M - 2, \dots, 2, 1$$
  
3. Adjustment Parameters

$$\begin{cases} W_{m}(k+1) = W_{m}(k) - \alpha S_{m}(k)(a_{m-1}(k))^{T} \\ b_{m}(k+1) = b_{m}(k) - \alpha S_{m}(k) \end{cases}$$
(7)

 $m = 1, 2, \dots, M - 1, M$ 

Where, P is input vector, T is output vector, M is the number of network layers and S is vector of system's sensitivity. It can be concluded that M=3 and in hidden layer of sigmoid function is as the following equation (8):

$$sig(n) = \frac{1}{1 + e^{-cn}}$$
 (8)

Where, C's value was chosen to be 1, and motive sigmoid function was considered linear, in equation (9): lin(n) = n

(9)

#### SIMULATION

For network learning, some input vectors (P) and some output vectors (t) are needed. Simulation is performed as in the following cases considering extracted data that is related to the two various types of 63/20kV and 132/20kV transformers from IRAN-TRANSFO Co..

TABLE II

### CASE STUDY I: Transformer 63/20kV

Table II and III are present 25 input vector and 25 output vector that are used for network learning.

INPUTS FOR TRASFORMER 63/20 kV					
Inputs	Short circuit impedance percent	Installation height	Volt per turn	Environment temperature	
P <sub>1</sub>	8	1000	87.719	50	
P <sub>2</sub>	10	1000	76.336	55	
P3	10	1000	84.034	50	
P <sub>4</sub>	10	1000	60.79	50	
P5	10	1000	68.027	45	
P <sub>6</sub>	12	1500	68.027	40	
<b>P</b> <sub>7</sub>	12	2200	54.795	40	
P <sub>8</sub>	12.5	1364	99.502	50	
P9	12.5	1500	54.201	40	
P <sub>10</sub>	12.5	1500	67.34	40	
P <sub>11</sub>	12.5	1500	76.923	50	
P <sub>12</sub>	12.5	1500	86.207	45	
P <sub>13</sub>	12.5	1500	106.952	45	
P <sub>14</sub>	12.5	1700	97.087	45	
P <sub>15</sub>	12.5	1900	49.948	39	
P <sub>16</sub>	13	2000	66.67	50	
P <sub>17</sub>	13.5	1000	79.94	47	
P <sub>18</sub>	13.5	1500	75.76	45	
P <sub>19</sub>	13.5	1500	75.785	40	
P <sub>20</sub>	13.5	1700	37.88	40	
P <sub>21</sub>	13.5	1700	47.17	55	
P <sub>22</sub>	13.5	1700	66.007	42	
P <sub>23</sub>	13.5	2000	46.62	50	
P <sub>24</sub>	13.7	1500	75.753	55	
Par	14	1000	121 212	45	

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Outputs	Weight of Iron	Weight of Oil	Weight of Copper			
t <sub>1</sub>	31200	13500	7700			
t <sub>2</sub>	25600	11500	7770			
t3	27000	11400	7094			
t4	22100	8500	7000			
t5	22700	9900	6894			
t <sub>6</sub>	24000	10600	8000			
t <sub>7</sub>	15100	7500	4124			
t <sub>8</sub>	38000	18000	11720			
t <sub>9</sub>	15250	7700	8667			
t <sub>10</sub>	22400	10300	6891			
t <sub>11</sub>	30160	13700	10000			
t <sub>12</sub>	30800	14520	9120			
t <sub>13</sub>	45470	19000	14850			
t <sub>14</sub>	33200	14100	9765			
t <sub>15</sub>	17450	8800	6600			
t <sub>16</sub>	25562	11820	9700			
t <sub>17</sub>	28750	11850	8950			
t <sub>18</sub>	27500	11100	9500			
t <sub>19</sub>	25600	10630	7387			
t <sub>20</sub>	9500	7250	2780			
t <sub>21</sub>	16700	8900	6300			
t <sub>22</sub>	27000	12250	8479			
t <sub>23</sub>	15550	8550	5199			
t <sub>24</sub>	25400	12300	7550			
t <sub>25</sub>	53100	25500	17450			

# TABLE IIIOUTPUTS FOR TRANSFORMER 63/20 kV

After learning each network and converging of all weights and biases, each of weights and biases of proposed network layer will be as the following. The converging value of the network is considered to be  $\alpha = 0.01$ .

$$W_{1} = \begin{bmatrix} 7.4733 & -0.2554 & 44.9077 & 26.0491 \\ 9.9807 & -4.3346 & 105.7249 & 36.3415 \\ 39.2733 & 4.7433 & 113.1023 & 47.4160 \\ 7.0358 & 0.6368 & 44.4176 & 25.6579 \end{bmatrix}$$
$$W_{2} = \begin{bmatrix} 16.6983 & 16.8123 & 41.5289 & 16.5226 \\ 3.0072 & 22.3003 & 3.1627 & 2.9944 \end{bmatrix}$$
$$W_{3} = \begin{bmatrix} 15.0497 & 25.7060 \\ 4.3241 & 12.3528 \\ 3.1704 & 8.7594 \end{bmatrix}$$
$$b_{1} = \begin{bmatrix} -7.3453 \\ -16.2992 \\ -12.3578 \\ -7.2830 \end{bmatrix}$$
$$b_{2} = \begin{bmatrix} -2.1148 \\ -4.4492 \end{bmatrix}$$
$$b_{3} = \begin{bmatrix} 10.9421 \\ 6.9762 \\ 4.7545 \end{bmatrix}$$

The learning curve is shown in Fig. 3. In this figure mean squared error decreasing by increasing the number of repeats is illustrated.



Fig. 3. Mean Square Error

# CASE STUDY II: Transformer 132/20kV

In table IV and V, 20 input vector and 20 output vector that are used for network learning.

TABLE IVINPUTS FOR TRASFORMER 132/20 kV

Inputs	Short circuit impedance percent	Installation height	Volt per turn	Environment temperature
P <sub>1</sub>	11.5	1000	79.635	52
P <sub>2</sub>	12	1000	106.383	50
P <sub>3</sub>	12	1000	120.043	48
P <sub>4</sub>	12	1000	130.36	48
P <sub>5</sub>	12.5	1000	60.606	50
P <sub>6</sub>	12.5	1000	87.858	48
P <sub>7</sub>	12.5	1000	97.777	48
P <sub>8</sub>	12.5	1350	88.106	40
P <sub>9</sub>	12.5	1350	90.09	40
P <sub>10</sub>	12.5	1500	44.15	45
P <sub>11</sub>	12.5	1500	60.423	45
P <sub>12</sub>	12.5	1500	98.039	45
P <sub>13</sub>	12.5	1500	116.279	40
P <sub>14</sub>	12.5	1700	90.909	45
P <sub>15</sub>	12.5	1700	114.286	45
P <sub>16</sub>	12.5	2000	91.05	40
P <sub>17</sub>	13.5	1000	105.8	50
P <sub>18</sub>	14	1000	80.829	48
P <sub>19</sub>	16	1000	151.554	48
P <sub>20</sub>	17	1000	168.394	48

TABLE VOUTPUTS FOR TRANSFORMER 132/20 kV

Outputs	Weight of Iron	Weight of Oil	Weight of Copper
t1	26700	14100	6900
t <sub>2</sub>	43700	16700	10184
t3	49200	22650	13120
t <sub>4</sub>	54300	29000	13800
t <sub>5</sub>	18500	11250	4700
t <sub>6</sub>	32700	20700	8570
t <sub>7</sub>	40000	22000	12000
t <sub>8</sub>	27500	15480	6910
t9	15400	15400	8877
t <sub>10</sub>	13500	11500	2755
t <sub>11</sub>	18000	11800	4567
t <sub>12</sub>	34300	15950	8900
t <sub>13</sub>	47350	22850	13000
t <sub>14</sub>	28800	15500	6725
t <sub>15</sub>	38750	16500	9750
t <sub>16</sub>	29250	15500	6730
t <sub>17</sub>	43000	20000	12200
t <sub>18</sub>	33680	21050	9700
t <sub>19</sub>	66330	31050	16500
t <sub>20</sub>	80350	37500	22670

After learning each network and converging of all weights and biases, each of weights and biases of proposed network layer will be as the following. The converging value of network has been considered to be  $\alpha = 0.01$ .

$$W_{1} = \begin{bmatrix} -2.7499 & 0.7275 & -20.3354 & -17.4651 \\ 4.8489 & -3.8294 & 44.5921 & 33.1134 \\ 2.2035 & 0.9106 & 28.6825 & 11.8429 \\ 0.0209 & 1.6786 & -25.5563 & -19.8255 \end{bmatrix}$$
$$W_{2} = \begin{bmatrix} 4.9226 & -22.6422 & -8.9358 & 3.9326 \\ -6.3882 & 1.8057 & 6.9438 & -9.0265 \end{bmatrix}$$
$$W_{3} = \begin{bmatrix} -29.6329 & 57.7119 \\ -8.2798 & 27.8681 \\ -7.7906 & 15.8360 \end{bmatrix}$$
$$b_{1} = \begin{bmatrix} 0.4064 \\ -8.5438 \\ -6.5073 \\ 1.1257 \end{bmatrix}$$
$$b_{2} = \begin{bmatrix} 0.2839 \\ -2.0211 \end{bmatrix}$$
$$b_{3} = \begin{bmatrix} 42.7250 \\ 19.7424 \\ 11.3507 \end{bmatrix}$$

The learning curve is shown in Fig. 4. In this figure mean squared error decreasing by increasing the number of repeats is illustrated.



Fig. 4. Mean Square Error

#### TRANSFORMER DESIGN

A new method which is based on cost estimating is presented as following in equation (10).

$$f = c_1 w_i + c_2 w_o + c_3 w_c + c_4$$

(10)

Where  $c_1$ ,  $c_2$ ,  $c_3$  are the cost of iron, oil and copper of transformer per ton. And the value of  $w_i$ ,  $w_o$ ,  $w_c$  are obtained, applying properties of related transformer in neural network. The coefficient,  $c_4$  is constant which is related to manpower cost and other components of transformer.

As an example if we need to estimate transformer cost with the following characteristics with help of employing neural network, the equations for manufacturing cost point of view are as follow:

	Short circuit impedance percent	Installation h	eight Volt	per turn	Environment temperature	
	12	1200		80	45	
f = 23.3	$845c_1 + 10.327c_2 + 6.756c_3 + c_4$	for	63/20 <i>KV</i>			
f = 25.	$347c_1 + 12.183c_2 + 6.871c_3 + c_4$	for	132/20 <i>KV</i>			

#### CONCLUSION

Power transformers are one of the most important components of the power systems. Around 15% of investment in transmission system goes towards transformer and since the major amount of transformers costs is related to its raw materials, so it has a high importance in costs estimating process.

In this paper a new method to estimate transformers pricing (by a cost function) is presented. In the cost function weight of iron, oil and copper play a crucial role and are suggested by the neural network according to the last four years of data from the transformers made by IRAN-TRANSFO Co.

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